

Cryogenics Course Material : 3-4

⌘ **Introduction : What is Cryogenics and Why Cryogenics for accelerator , Present Scenario**

⌘ **How to Generate low Temperature / Production of Cryogen : Thermodynamics / Refrigeration Cycle**

⌘ **How to Store & Transfer Cryogen : Heat transfer, Cryomodule Design, Properties of Material :**

⌘ **Measurement at Low temperature :**

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CRYOGEN STORAGE VESSEL, CRYOSTAT & Transfer Line



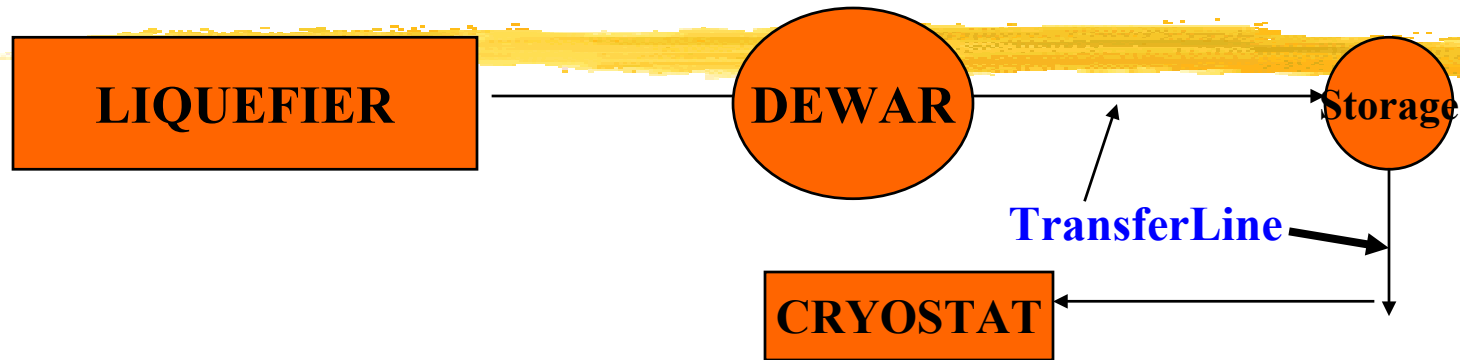
⌘ **INTRODUCTION**

⌘ **DIFFERENT MODES OF HEAT TRANSFER**

⌘ **TECHNIQUE TO REDUCE IT (Cryogenic Insulation)**

⌘ **PROPERTIES OF MATERIAL AT LOW TEMPERATURE (DESIGN FACTOR)**

CRYOGEN CYCLE



STORAGE VESSEL : To Store liquid Nitrogen, liquid Helium, Liquefied Natural Gas (LNG) at their Boiling Point (Fixed T)
Capacity : 5 litres to 500,000 litres

Transfer line : To Transfer Cryogen from one point to another

Cryostat : To Carry out Expt at low temperature (Variable T)

Both need good Insulation ($T_r - T_b$) Higher

WHY STORAGE IS SO CRITICAL

A. LOW LATENT HEAT

B. LARGE TEMPERATURE DIFFERENCE

Property	He	H ₂	N ₂	Water
Boiling Point	4.2K	20K	78K	373K
Density	0.12kg/liter	0.07kg/ litre	0.81kg/litre	1kg/litre
<i>Heat of Vaporisation</i>	<i>20KJ/ kg</i>	<i>428</i>	<i>198</i>	<i>2250</i>
Liquid evaporated on 100 W Heat input	140 l/ hr	12 l/hr	2.2 l/hr	0.16 l/hr

1 W HEAT LOAD EVAPORATES 34 LITRES Lhe in ONE DAY

THANKS TO MLI (MULTILAYER INSULATION TECHNOGY)

EVAPORATION RATE ONLY 1 LITRES/DAY

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HEAT TRANSFER TO CRYO VESSEL/ CRYOSTAT

Simple Configuration

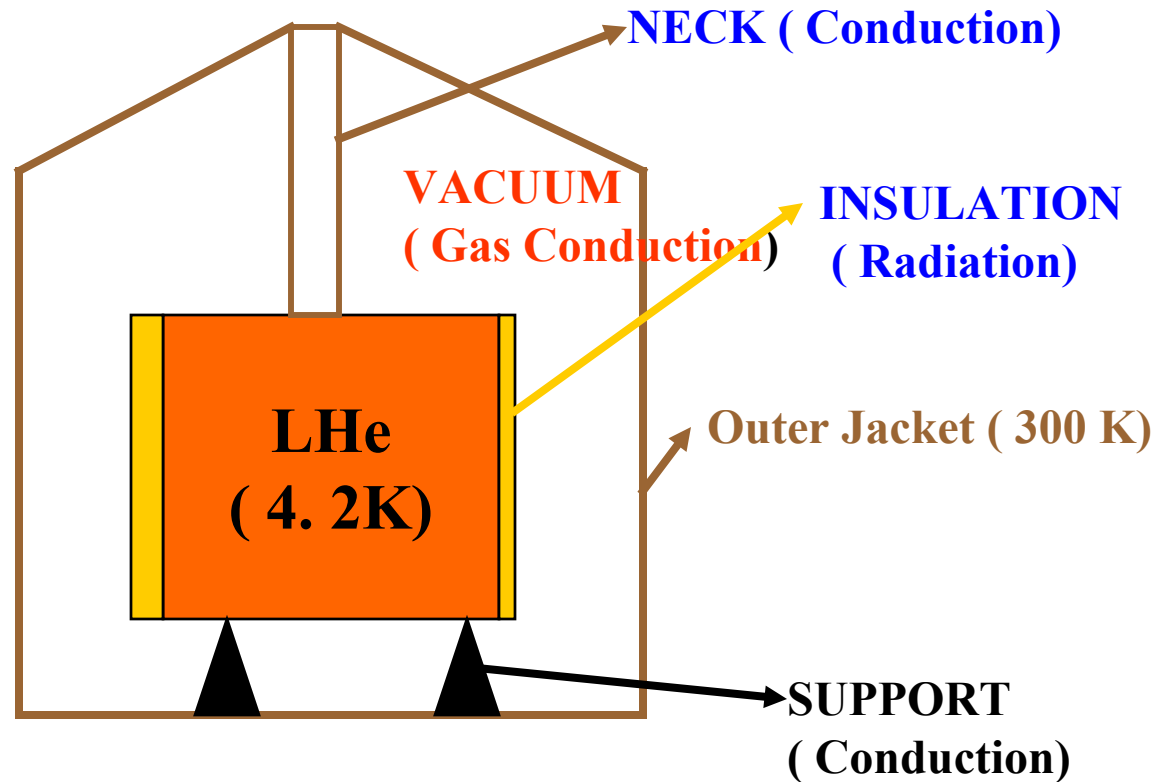
Design Goal :

Reduce Heat Flux
from Outside

Structural Stability

Avoid Collapsing

Safety Features



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The 3 modes of heat transfer

- ⌘ **Conduction: heat transported in solids or fluids at rest**

$$Q = -k(T)A \text{ grad } T$$

FOURIER's law:

- ⌘ **Convection: heat transport produced by flow of fluid**

$$Q = hA(T_w - T_f)$$

Convection exchange:

- ⌘ **Radiation: heat carried by electromagnetic radiation**

Stefan-Boltzmann's law:
$$Q = \sigma \varepsilon A (T_h^4 - T_c^4)$$

HEAT TRANSFER MECHANISM

A. Solid conduction heat transfer : *Necktube, Support structure .*

B. Radiation heat transfer : *Through vacuum*

C. Gas conduction : *Residual gas in the vacuum space.*

Solid Conduction :

$$Q_c = K_m (A_c / L) (T_h - T_c)$$

A_c = Cross sectional area (example for a rod of dia (d), $A_c = \pi d^2/4$,

Similarly for a pipe of outer diameter d and thickness 't', $A_c = \pi dt$)

L = Length of rod/ pipe,

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Conductivity $k_m = F(T)$ $k_m = \left[\int_c k dT / (T_h - T_c) \right]$

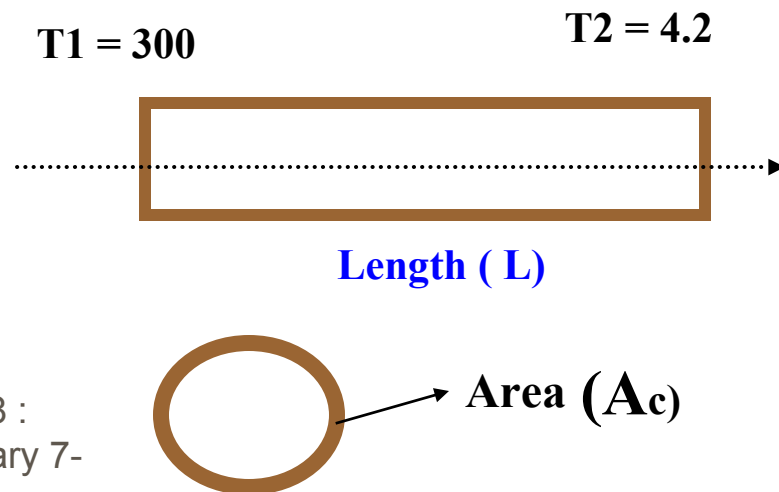
$Q_c = (A_c / L) \int_c k dT.$

Conductivity integral value of stainless steel between 300K and 80 K is evaluated by

$\int_{80}^{4.2} k dt = \int_{300}^{4.2} kdT - \int_{80}^{4.2} kdT = (30.6 - 3.49) = 26.1 \text{ W/ cm}$

CONDUCTION REDUCED BY;

- 1. Low Croosectional Area
- 2. Long Length
- 3. Low conductivity pipe (SS/ FRP)
- 4. Thermal interception



Thermal conductivity integrals

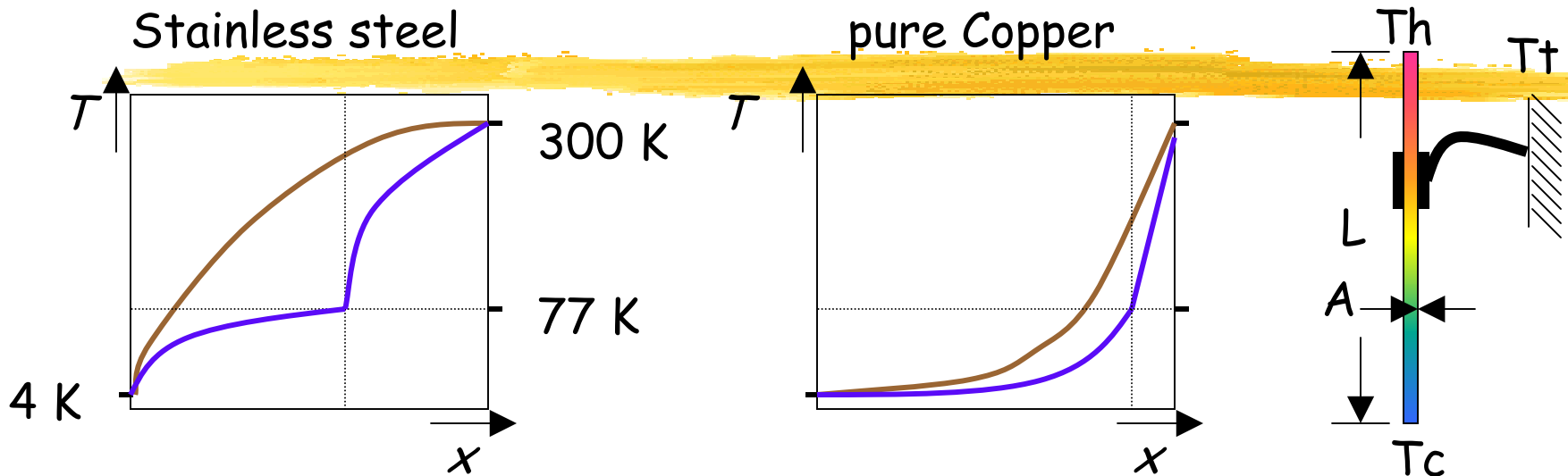
$T_c = 4 \text{ K}$

T_2	ETP copper	Aluminium 1100	Austenitic stainless steel	Glass	PTFE
[K]	[W cm ⁻¹]	[W cm ⁻¹]	[W cm ⁻¹]	[mW cm ⁻¹]	[mW cm ⁻¹]
10	33.2	6.07	0.0293	6.81	4.4
20	140	27.6	0.163	20.0	16.4
30	278	59.2	0.424	36.8	32.3
40	406	96.2	0.824	58.6	50.8
50	508	134	1.35	84.6	71.6
60	587	170	1.98	115	93.6
70	651	202	2.70	151	116
80	707	232	3.49	194	139
90	756	258	4.36	240	163
100	802	284	5.28	292	187
120	891	330	7.26	408	237
140	976	376	9.39	542	287
160	1060	420	11.7	694	338
180	1140	464	14.1	858	390
200	1220	508	16.6	1030	442
250	1420	618	23.4	1500	572
300	1620	728	30.6	1990	702

⌘ Reduction of heat flow to the cold boundary temperature by thermal interception at intermediate temperature

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Intermediate heat interception



Example : SS tube Structure (2.54 Cm x 1mm x 1 m length) (300- 4.2 K)

No Thermal interception $Q = 0.24 \text{ W}$ ($3.14 \times 2.54 \times .1 \times 30.6/100$)

80 K Thermal Interception at 70 Cm, $Q = 0.04\text{W}$ ($3.14 \times 2.54 \times .1 \times 3.49/ 70$)

80 K Thermal Interception at 10 Cm , $Q = 0.27\text{W}$ ($3.14 \times 2.54 \times .1 \times 3.49/ 10$)

Refrigeration properties of cryogenes

Working domain close to critical point:

properties of liquid and vapor phase are similar

low vaporization heat

Low viscosity hence excellent leaktightness required for He

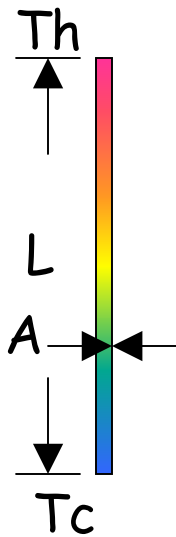
		He	N ₂	H ₂ O
Normal boiling Pt		4.2	77	373
Critical temperature		5.2	126	647
Critical pressure		2.3	34	221
Liquid density/ Vapor density*		7.4	175	1600
Heat of vaporization	[Jg ⁻¹]	20.4	199	2260
*Liquid viscosity *	[μpoise]	3.2	152	283
Enthalpy increase between T ₁ and T ₂	T ₁ = 4.2 K	384	-	-
	T ₂ = 77 K			
	T ₁ = 4.2 K	1157	228	-
	T ₂ = 300 K			

*at normal boiling point

highly effective for self-sustained vapor cooling!

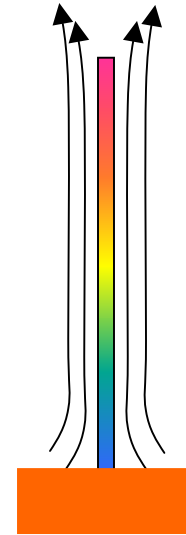
Shielding potential of cold vapours

Pure conduction heat losses evacuated at the coldest temperature



$$\dot{Q} = \frac{A}{L} \int_{T_1}^{T_2} k(T) dT$$

Self sustained vapour cooling: vapour flow generated only by heat leak is used to cool the device



Heat evacuation across a small ΔT thermodynamically much more efficient

Shielding potential of cold vapours

heat balance, perfect exchange

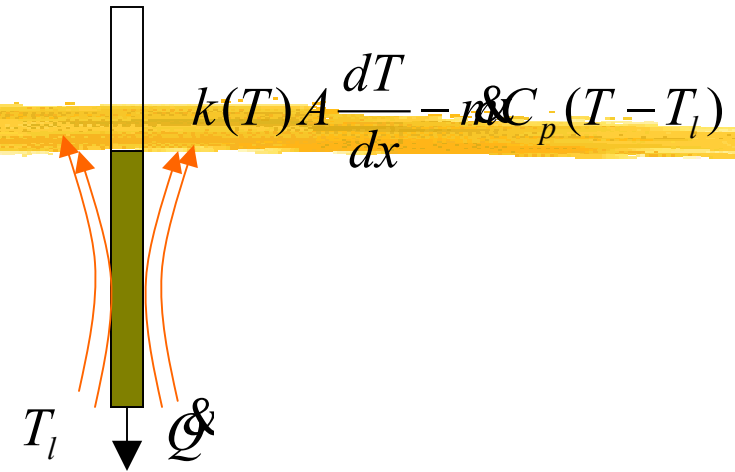
$$\dot{Q} = k(T)A \frac{dT}{dx} - \dot{m}C_p(T - T_l)$$

self-sustained evaporation of fluid

$$\dot{Q} = \dot{m}L_v$$



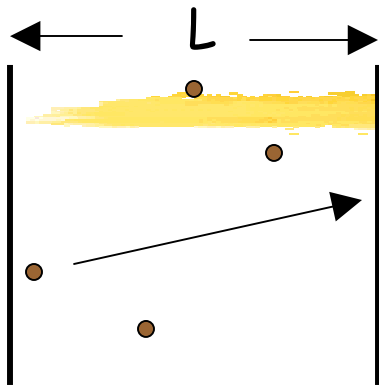
$$\dot{Q} = \frac{A}{L} \int_{T_l}^{T_2} \frac{k(T)dT}{1 + (T - T_l)C_p / L_v}$$



$$\dot{Q} = \frac{A}{L} \int_{T_l}^{T_2} k(T)dT$$

Th.conductivity integral	[W cm ⁻¹]	[W cm ⁻¹]
ETP copper	128	1620
OFHC copper	110	1520
Aluminium 1100	39.9	728
AISI 300 st.steel	0.92	30.6

Conductivity of gases:



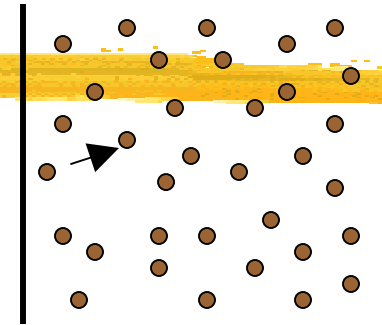
mean free path

vs

wall distance L

$$\lambda = 115 \cdot \frac{\mu}{p} \sqrt{\frac{T}{M}}$$

[Pa.s],[Pa],[cm]



molecular:

q proportional to p
q independent from L

viscous:

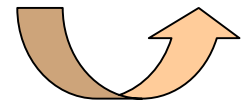
q independent from p
q = kSΔT/L
k predicted by kinetic theory of gases

P [Pa]	10 ⁻²	100
Ar	0.63 cm	6.3 · 10 ⁻⁵
N ₂	1.8	1.8 · 10 ⁻⁴
He	0.60	6.0 · 10 ⁻⁵

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$$k = \frac{1}{3} \rho \left(\frac{8RT}{\pi M} \right)^{\frac{1}{2}} \lambda C_v$$

$$k \sim T^{0.7}$$



Molecular regime: Kennard's law

$$\gamma = C_p / C_v$$

$$Q = A_1 \alpha \left(\frac{\gamma + 1}{\gamma - 1} \right) \left(\frac{R}{8\pi} \right)^{1/2} \frac{p}{\sqrt{MT}} (T_2 - T_1)$$

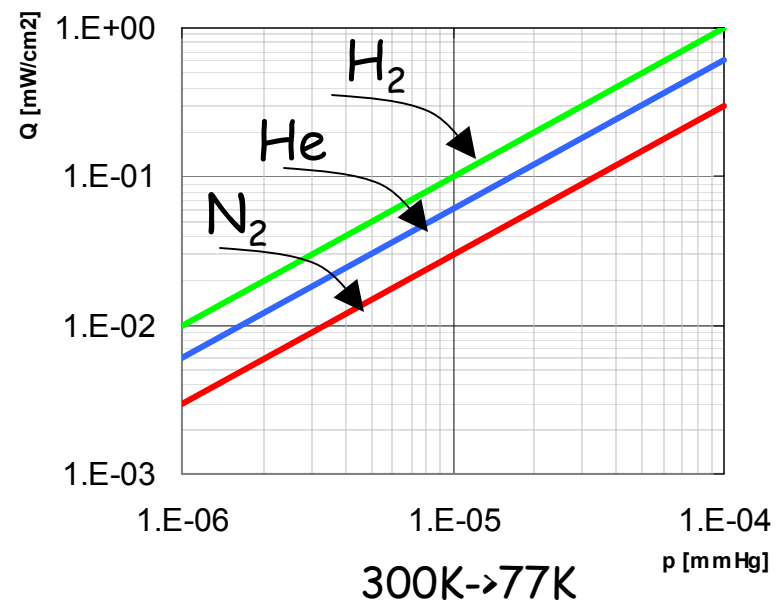
R ideal gas constant

α accommodation coefficient

$0 < \alpha < 1$, degree of thermal equilibrium between molecules and wall, $\alpha \sim 0.7-1$ for heavy gases.

$$\alpha = \frac{\alpha_1 \alpha_2}{\alpha_2 + \alpha_1 (1 - \alpha_2)} \frac{A_1}{A_2}$$

for simple geometries,
(parallel plates, coaxial
cylinders, spheres)



Residual gas conduction :

At lower pressure : Mean Free Path of the molecules >> ANNULAR GAP

$$Q_{gc} = C \alpha P (T_h - T_c)$$

C = constant, α = accommodation coefficient, P = Gas pressure

Residual gas conduction can be reduced

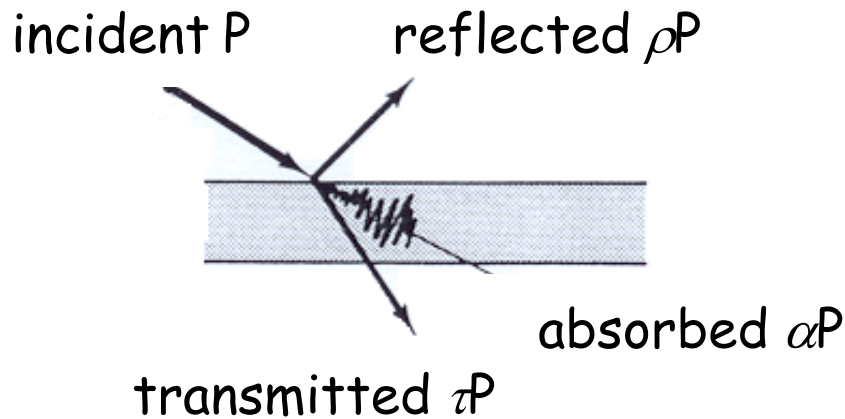
1. Clean surface (low α) 2. by high vacuum.

<i>Gas</i>	<i>C</i>	<i>α</i>	<i>P (Torr)</i>	<i>T2/T1</i>	<i>Qgc (W/m²)</i>
Air	0.02	0.8	10⁻⁵	300/78	0.35
Air	0.02	0.8	10 ⁻⁵	78/4.2	0.11
Air	0.02	0.8	10⁻³	300/78	35
Helium	0.03	0.35	10 ⁻⁵	300/4.2	0.31
Helium	0.03	0.35	10 ⁻⁵	78/4.2	0.07

RADIATION

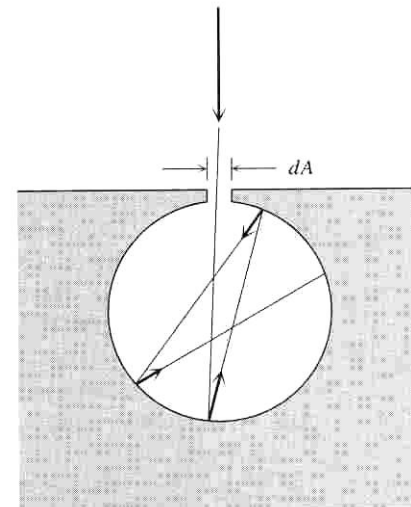
Any surface $T > 0\text{K}$ absorbs (α) and emits (ε) energy as electromagnetic radiation:

depending on direction and wavelength



BLACK-BODY:

The whole incident radiation is absorbed: $\alpha=1$



Energy conservation $\rho + \alpha + \tau = 1$

Opaque medium $\rho + \alpha = 1$

Heat transfer between 2 real surfaces

$$q = \sigma A_1 \epsilon_{12} (T_2^4 - T_1^4) \quad \epsilon_{12} \text{ effective emissivity (emissivities + view factor)}$$

Parallel plates

$$\frac{\epsilon_1 \epsilon_2}{\epsilon_2 + (1 - \epsilon_2) \epsilon_1}$$

Spheres and long cylinders

$$\frac{\epsilon_1 \epsilon_2}{\epsilon_2 + \frac{A_1}{A_2} (1 - \epsilon_2) \epsilon_1}$$

self-contained, not concentric/coaxial

(A1 < A2)

A₂ >> A₁ equivalent to A₂ black: black-body radiation fills the cavity between the two surfaces and is collected by A₁ proportionally to ε₁

Radiation :

*For vacuum insulation, the dominant contribution to heat inleak into a storage vessel or cryostat is **Radiation***

Radiant heat transfer rate between two parallel surfaces

$$Q_r = F_{e1-2} F_{1-2} \sigma A_1 (T_1^4 - T_2^4)$$

F_{e1-2} = Effective emmissivity, F_{1-2} = Geometry factor = 1, σ = Stefan

Boltzman constant = 5.6×10^{-8} w/m² K. A_1 = Surface area of inner vessel.

$1/F_{e1-2} = 1/e_1 + A_1/A_2 (1/e_2 - 1)$, **e : emmissivity for inner and outer surface.**

Radiation Heat transfer is reduced by :

1. *Intermediate thermal shield*

Liquid helium/ hydrogen vessel : liquid nitrogen cooled shield

heat transfer reduction : by a factor of $200 \sim (300/80)^4$

2. *Material of low emmissivity : by electropolishing or aluminum tape.*

SS : 0.34, SS (Mech. Polished) : 0.12, SS (Elec. Polish) : 0.1

SS + Al Foil : 0.056, Copper : 0.12 : Careful on Oxide formation

3. *Optimizing the surface area for a fixed volume.*

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Heat Transfer for Vacuum Insulation on bare Polished SS surface (Radiation)

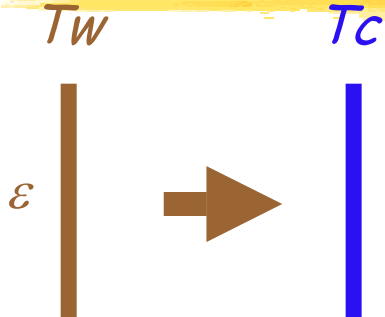
T_2 (K)	T_1 (K)	Heat flux (W/m^2)	Evaporation rate (l/hr)
300	78	45	1 litre/hr liquid Nitrogen
200	78	9	0.2 litre/hr
300	20	45	5 litres/ hr liquid Hydrogen
80	20	0.23	0.026 litre/hr
300	4.2	45	65 litres/hr liquid Helium
80	4.2	0.23	0.33 litres/hr

Standard Helium Dewar of 100 litres : Evaporation < 1 litres/ day

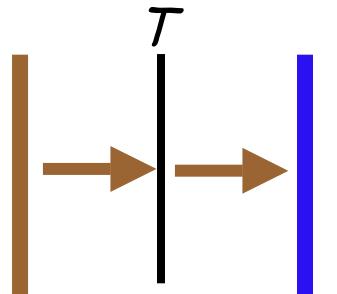
Floating radiation screens

Floating = not actively cooled, they operate at a temperature determined by heat balance

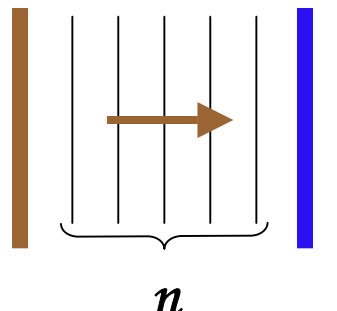
T_w T_c



$$\phi = \left(\frac{\sigma \varepsilon}{2 - \varepsilon} \right) (T_w^4 - T_c^4)$$



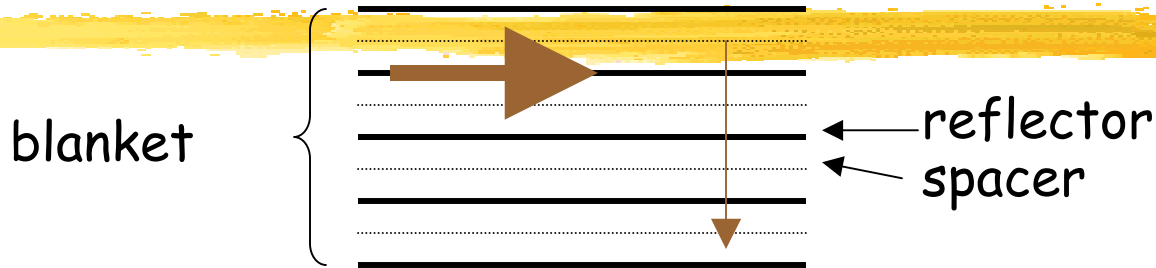
$$\phi = \frac{1}{2} \left(\frac{\sigma \varepsilon}{2 - \varepsilon} \right) (T_w^4 - T_c^4) \quad T^4 = \frac{1}{2} (T_w^4 + T_c^4)$$



$$\phi = \frac{1}{n+1} \left(\frac{\sigma \varepsilon}{2 - \varepsilon} \right) (T_w^4 - T_c^4) \quad T_i^4 = T_c^4 + \frac{T_w^4 - T_c^4}{i+1}$$

Multi-layer Insulation

Stacking of "reflectors" separated by insulating "spacers"



Reflector: low emittance radiation shield

polyester film, 300-400 Å pure Al coating, usually double face

Spacer: insulating, lightweight material

paper, silk, polyester net

1. Heat transfer parallel to the layers ~ 1000 times greater than normal to the layers

thermal coupling between blanket edges and construction elements may dominate heat rate.

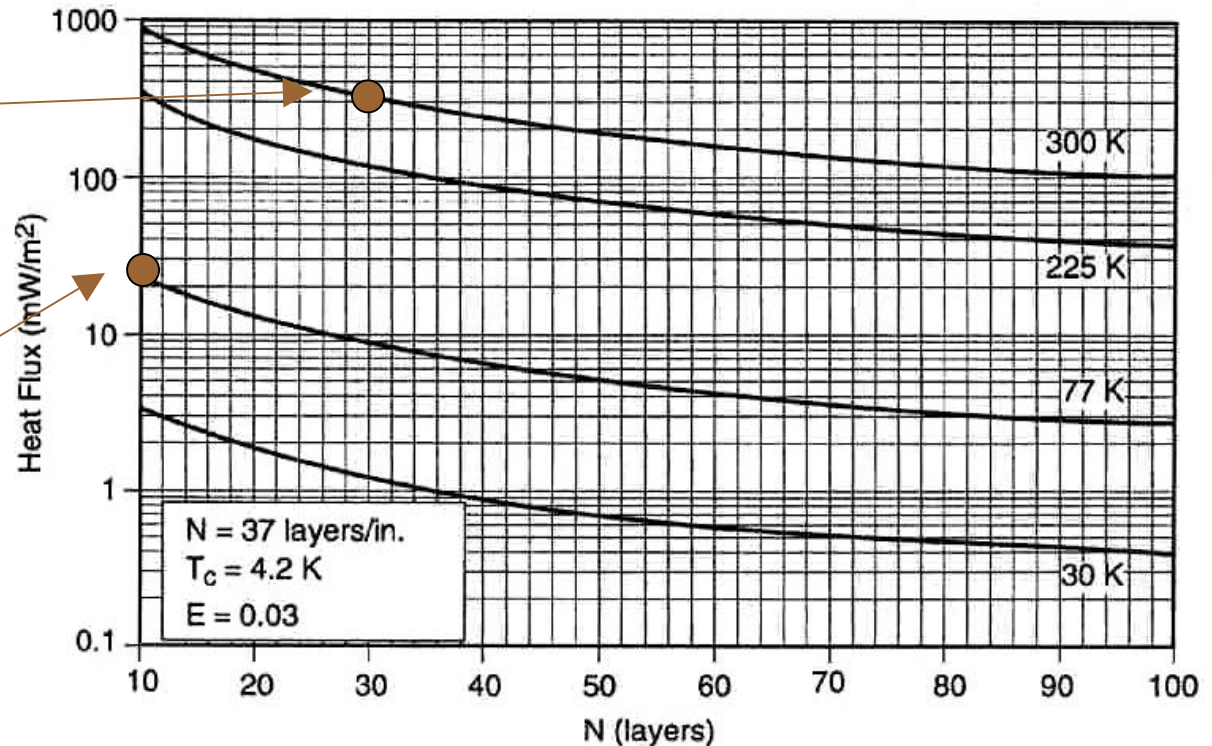
2. Heat transfer very sensitive to layer density

single local compression affects the T profile over the entire blanket, substantially degrading heat loss (factors 2-3 more !)

MLI: number of layers

30 layers,
300K → 77K,
0.5 W/m²

10 layers,
77K → 4K,
20 mW/m²



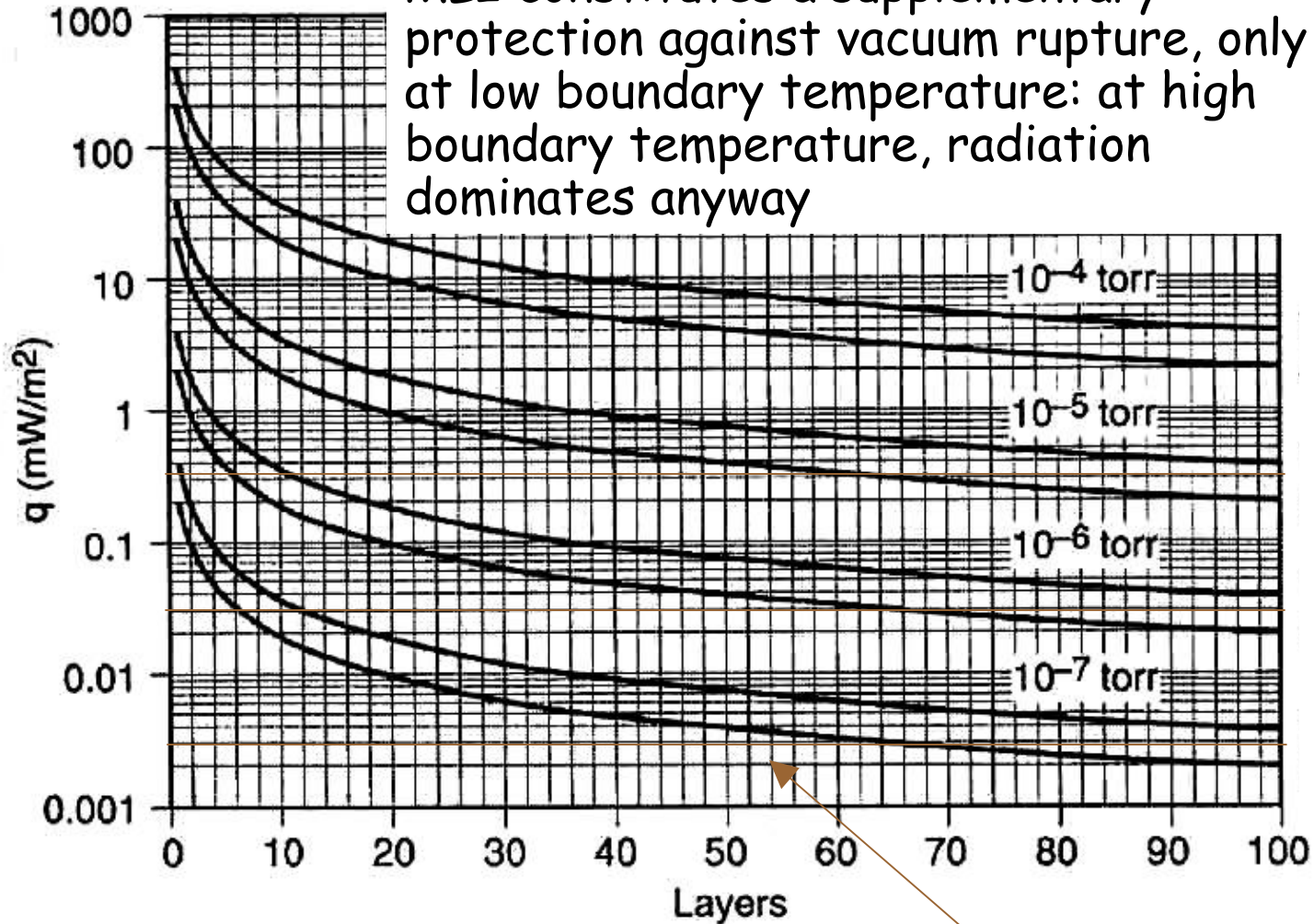
$$N = 15 \text{ cm}^{-1}$$

$$T_c = 4.2 \text{ K}, \epsilon = 0.03$$

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MLI and residual pressure

MLI constitutes a supplementary protection against vacuum rupture, only at low boundary temperature: at high boundary temperature, radiation dominates anyway



interstitial
gas:
nitrogen

300 K -> 77 K

77 K -> 4.2 K

300 K -> 77 K

77 K -> 4.2 K

300 K -> 77 K

77 K -> 4.2 K

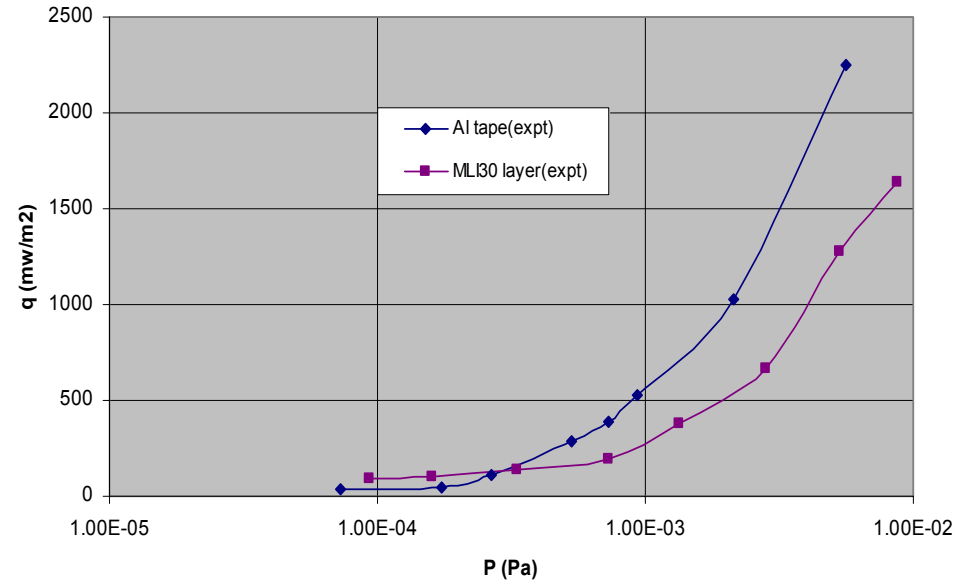
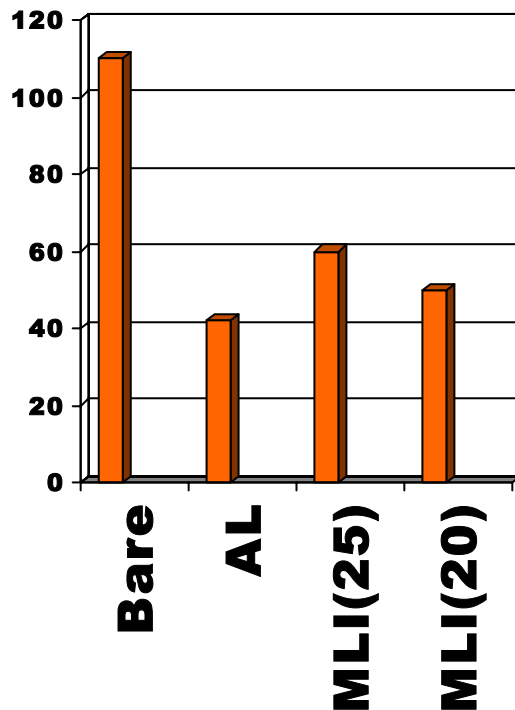
300 K -> 77 K

77 K -> 4.2 K

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Performance Comparison of Al tape and MLI w.r.t Vacuum (80- 4.2 K)

LOAD (mw/m²) : 80- 4.2 K



Heat load measurement repeated with different vacuum (**5x 10⁻⁷ Torr to 5 x 10⁻⁴ Torr**) by using a fine leak valve of Pfeiffer

Conclusion : Performance of Al tape is better than MLI if Vacuum is better than 3 x 10⁻⁶ Torr

Multilayer Insulation (MLI)



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CRYOGENIC INSULATION

A. FOAM INSULATION (POLYSTYRENE, POLY URETHENE (PUF)

Aparant thermal Conductivity : 20 - 35 mw/ m.K

B. POWDER : (Evacuated Perlite Powder)

Aparant Thermal Conductivity : 1- 2 mw/ m. K

No radiation.

C. VACUUM ALONE (Only Radiation)

Ka : 5mw/ m. K at 10⁻⁶ torr

C. MLI (MULTILAYER) : Highly reflective Film with low conductivity spacer)

Ka = .002 - .005 mw/ m. K

All heat transfer is Minimised. $Q = \frac{\epsilon A (T_1^4 - T_2^4)}{2(N+1)}$

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Typical heat inleaks in a cryostat

...between flat plates, at vanishingly low temperature

	[W/m ²]
Black-body radiation from 290 K	400
Black-body radiation from 80 K	2.3
Residual gas conduction (100mPa helium) from 290 K	19
Residual gas conduction (1mPa helium) from 290 K	0.19
Multi-layer insulation (30 layers) from 290 K, pressure below 1mPa	0.5-1.5
Multi-layer insulation (10 layers) from 80 K, pressure below 1mPa	0.05
Multi-layer insulation (10 layers) from 80 K, residual pressure 100mPa	0.2
Residual Gas conduction (100mPa) from 80 K	6.8
Residual gas conduction (1mPa) from 80 K	0.07

A. Thermal Conductivity Integrals of common material

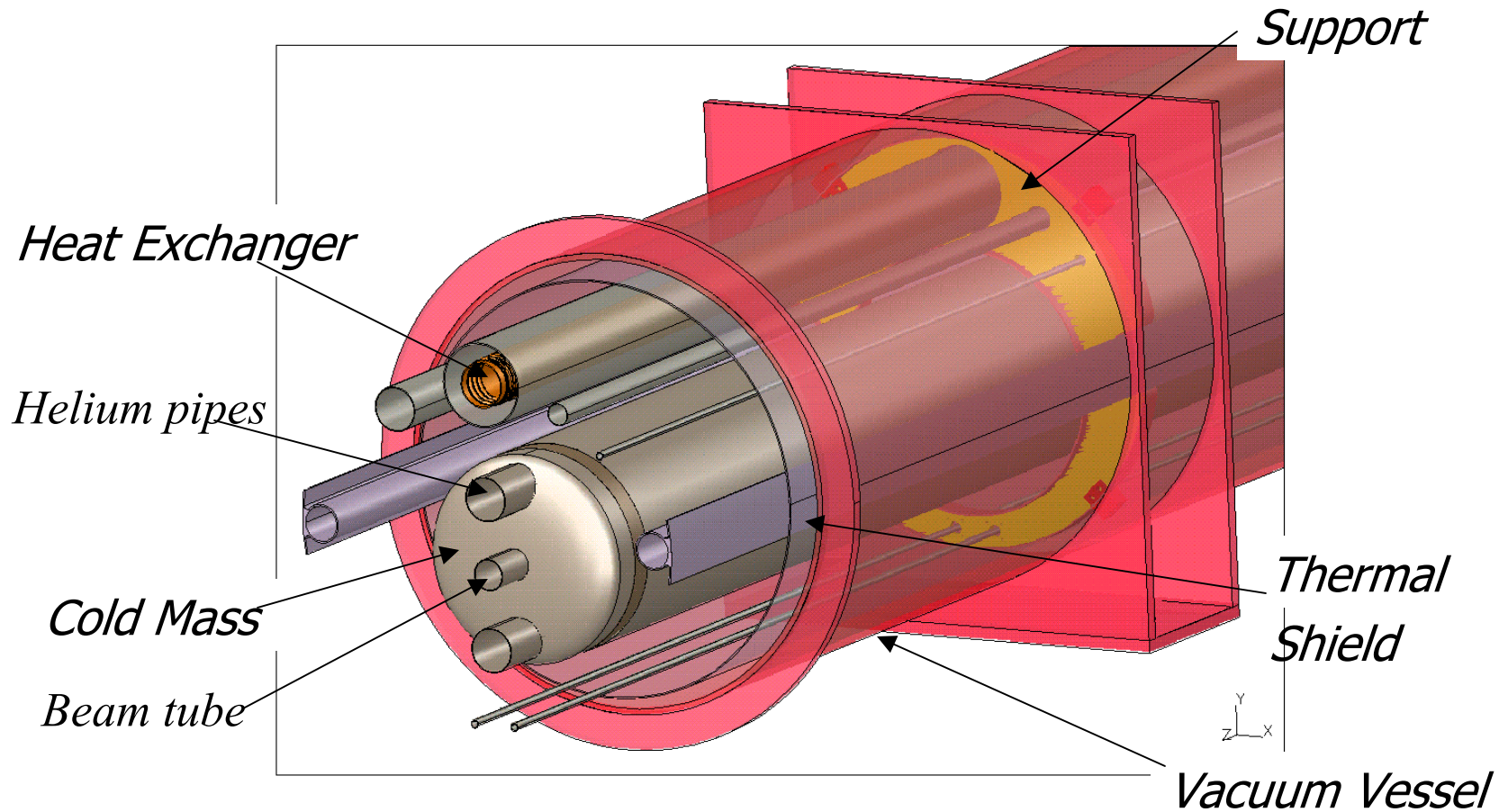
4.2 K To	80 K	300K
OFHC Copper	600 w/cm	1600
AISI 304 SS	3.49	30.6
G - 10	0.18	1.53

B : Emissivity of Technical materials

	300- 77K	77- 4.2K
SS as found	0.34	0.12
SS Mech polished	0.12	0.07
SS Electropolished	0.10	0.07
SS+ Al foil	0.05	0.01
Al Mech polished	0.10	0.06
Copper, Mech polished	0.06	0.02

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A superconducting accelerator magnet



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A super-conducting magnet built by Fermilab for LHC at CERN in Geneva, Switzerland

Consists of layers from cold inside to warm outside -- magnet, inner pipes, thermal insulation, steel vacuum container



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Summary of Heat Load Budget For Accelerator Cryomodule/ Distribution line

- Input Parameters :**
1. **Total length of Module (Meter)**
 2. **Surface area per unit length (M²/ M)**
 3. **Weight of Cold Mass/ m length**
 4. **Dynamic Load : Rf power, Magnet**

Whether we Need intermediate thermal shield ?

1. **Option one (No) : 30 layers of MLI , $Q = 2 \times 1.5 = 3W$**
2. **80 K Shield (No MLI) : $Q = 2 \times .15 = 0.3$ (one order less)**
3. **Same with one layers Al Foil $q = 2 \times .02 = 0.04 W$**

Vacuum Level ?

10⁻⁵ mbar $Q_g = 2 \times .07 = 0.15 W$

10⁻³ mbar , $Q_g = 2 \times 7 = 14 W$ (not acceptable)

Heat load Budget- 2

We have Seen 80 K shield+ 1 layers Al Foil and Vacuum better than 10- 5 mbar, Load from Radiation and gas conduction per m length

$$Q_g + Q_r = .03 + 0.15 = 0.19 \text{ W}$$

Same with vacuum 10-3 mbar, $Q = 15 \text{ W}$

If we wrap with 10 layers of MLI

$Q = 4 \text{ W}$ (Still higher but better than 15 W)

Generally Vacuum is better than 10-6 mbar unless there is a leak : This further reduces the heat load

Conclusion : 80 K Shield + 10 layers MLI + vacuum better than 10-5

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What About Conduction load ?

Heat load Budget- 3

Once we know the weight, we can easily calculate the Cross sectional Area Required for the load either in Compression or Tension mode

Two alternatives 1. SS 2. G 10

Thermal Interception (80 K) is required or not

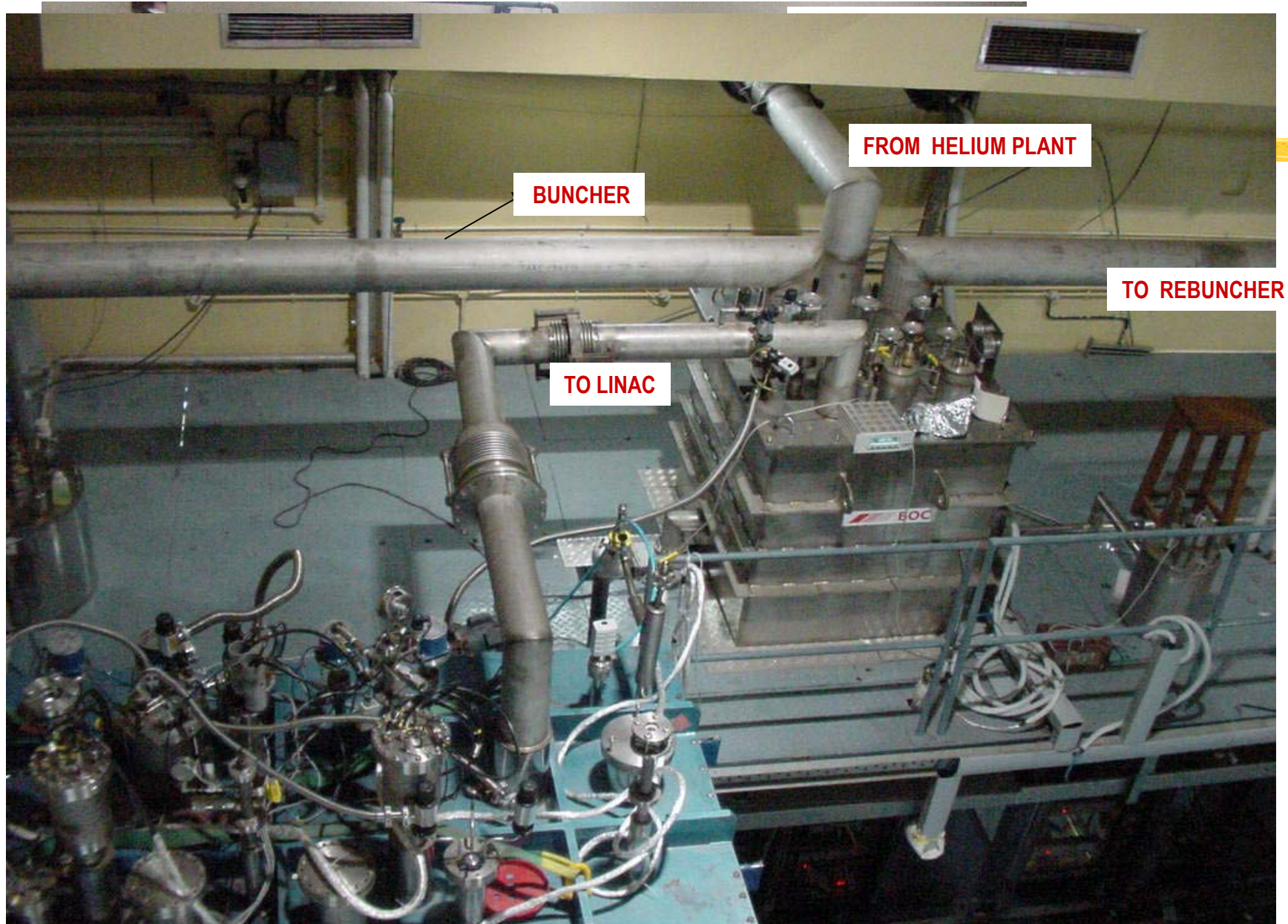
	SS	G-10
KdT (: 300- 4.2)	30.6 W/cm	1.53
KdT (80- 4.2)	3.49	0.18

Yield strength for both is almost same , so Cross sectional area remains same

G- 10 is even better without thermal interception than SS with 80 K thermal interception

G- 10 Difficulty on Fabrication, Cascade better and case to case

LIQUID HELIUM DISTRIBUTION NETWORK



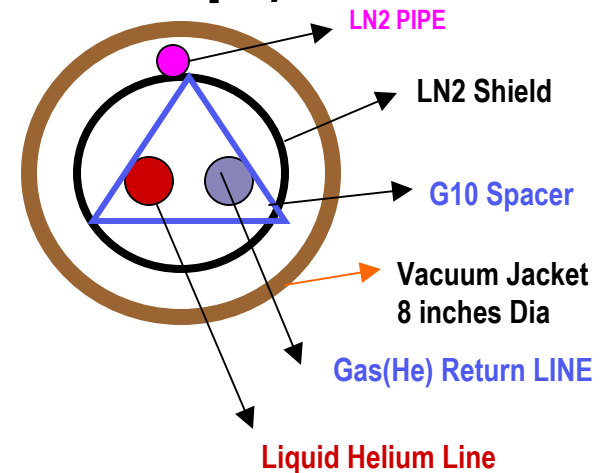
Specification of Lhe Distribution Network

⌘ **Four Valve boxes** : Weka valves, Vacuum break, Instrumentation, Rectangular & Circular shape, LN2 Shielded

⌘ Vacuum jacketed, MLI insulated, LN2 shielded Line, **40 meters length**.

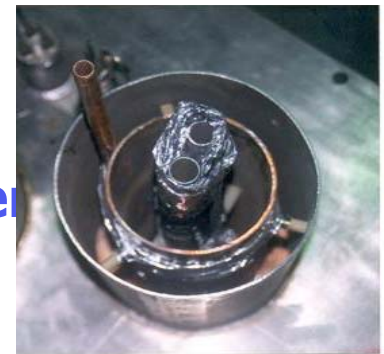
⌘ Demountable Joints to isolate line from Cryostats

⌘ Line without LN2 shielded

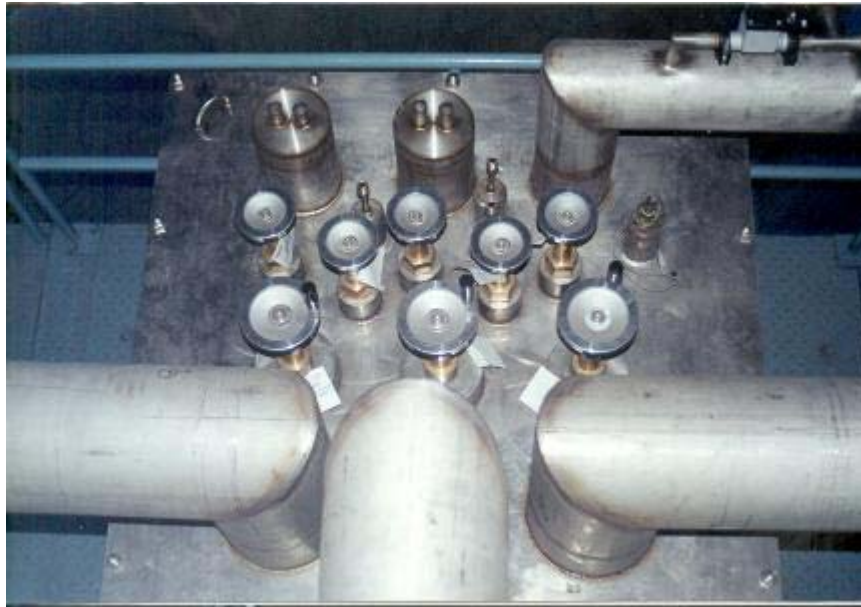


⌘ **MEASURED LOAD** : **21 W** in **23 meters** length

⌘ **Actual Load in Line** : **0.51 W/ m**



LIQUID HELIUM VALVE BOXES



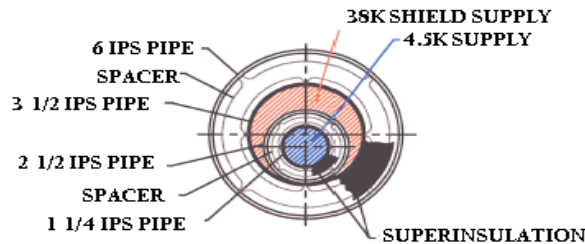
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JLab Designed MSU Distribution Box

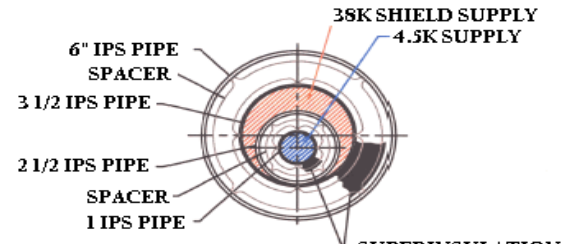


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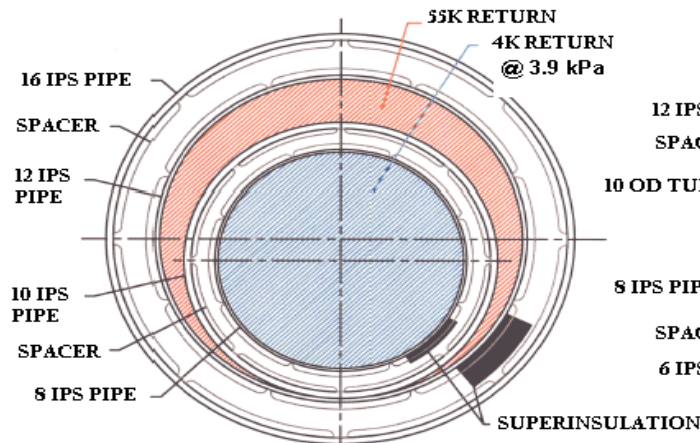
Transfer Line Cross sections (SNS)



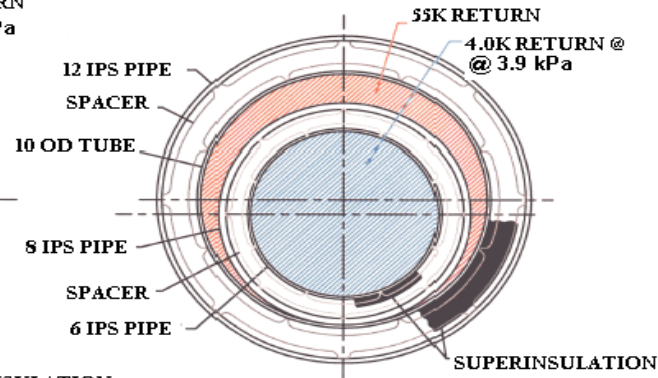
CHL SUPPLY TRANSFER LINE



LINAC SUPPLY TRANSFER LINE



CHL RETURN TRANSFER LINE



LINAC RETURN TRANSFER LINE

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JLab Transfer Line Bayonets



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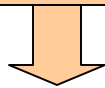
Designing and Developing any cryogenic apparatus like cryostats, experimental dewar require good knowledge of material properties at low temperature.

Why do you need to know ?

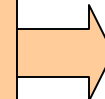
Most of the properties may vary by orders of magnitude between ambient and cryogenic condition

Why does the Property vary?

At room temperature the atoms are vibrating very rapidly. Higher the Temp. greater is the amplitude of Oscillation. As the substance is cooled down, the amp. Of atomic vibration is reduced (thermal energy reduces)



Thus all the properties which dependent on interactions with the atomic vibration (or Lattice) will change at low temperature



The decrease in the various types of interaction will show up as variation in the mechanical properties. Thermal properties and electrical properties

Properties Concerned

Mechanical

Ductility

Yield Strength

Ultimate Tensile strength

Electrical

Not so important as far as cryogenics is concerned

Thermal

Thermal Contraction

Thermal Conductivity

Specific Heat

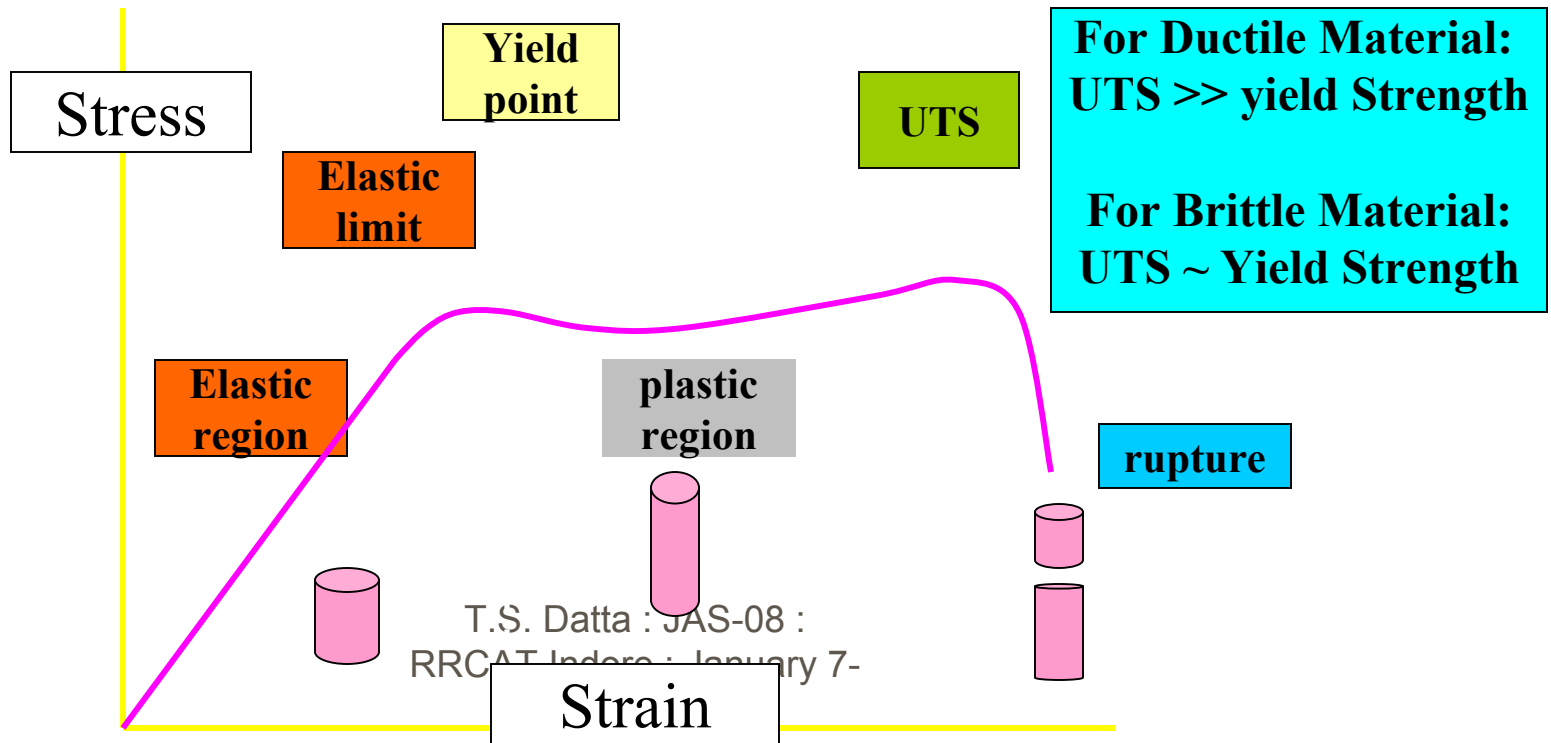
Mechanical Properties

Ductile -Brittle Behavior

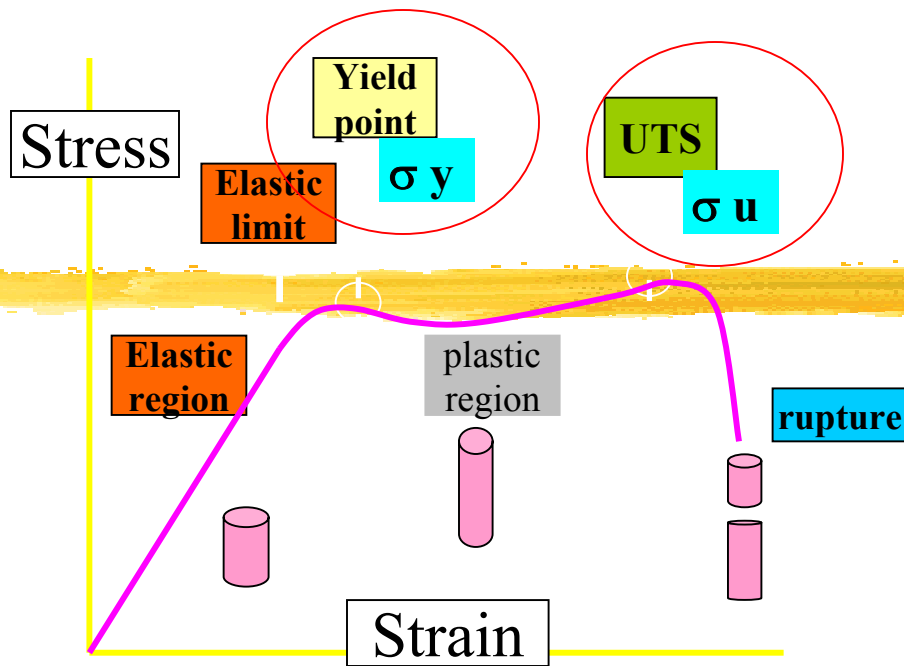
It

Yield Strength

Ultimate Tensile Strength [UTS]



Ductility



N/m ²	σ_y (4.2K)	σ_u (4.2K)	σ_y (80K)	σ_u (80K)	σ_y (300K)	σ_u (300K)
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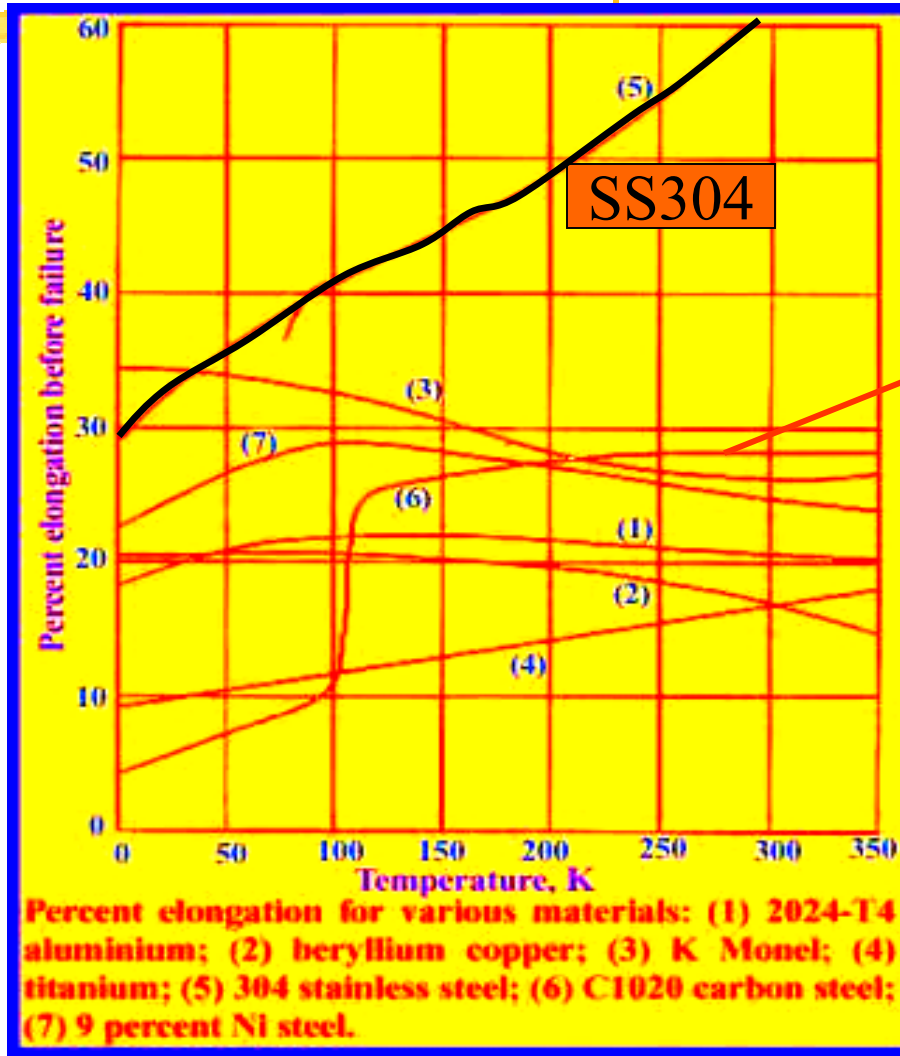
SS304	547	1660	460	1509	406	659
Al -6061	345	497	332	422	282	312
OFHC Cu	90	418	88	360	75	222
G-10	758	758	703	703	414	414

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Elongation Before Failure



**Carbon Steel
Became Brittle
at 120 K**

Thermal Properties

Thermal Contraction

Fractional Change in length per unit change in Temp.

Why do U require “ α ” ?

Thermal Contraction of different material vary considerably. Therefore differential thermal contraction has to be taken care of

Thermal expansion Coefficient



Thermal Properties

**Thermal
Contraction**

**Thermal
Conductivity**

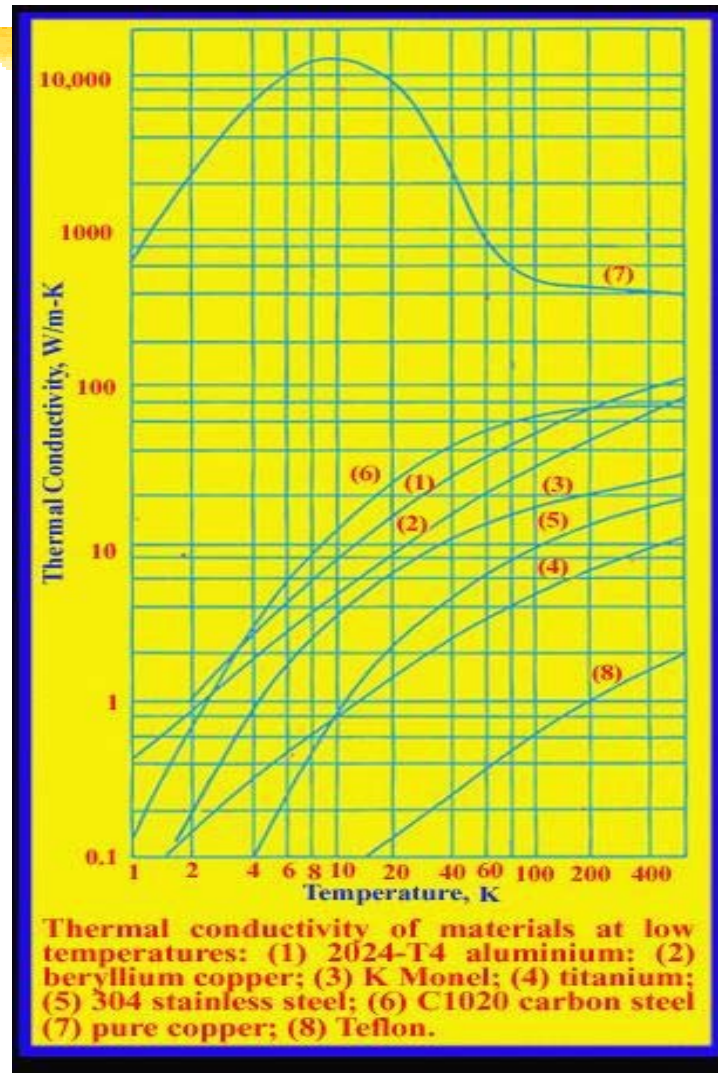
Heat transfer rate per unit area per unit thermal gradient which causes the heat flow

Why Do You Require “K” ?

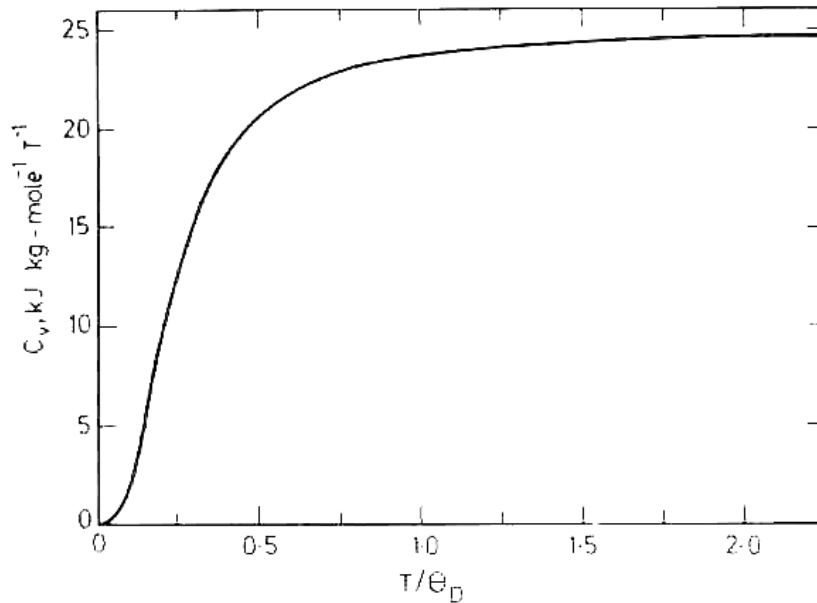
Q
↓
300K
4.2K

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Thermal Conductivity



Specific heat of structural materials



C_v heat capacity per kg mole approximately described by the

Debye function

$$C_v = 9R \left(\frac{T}{\theta_D} \right)^3 \int_0^{\theta/T} \frac{x^4 e^x}{(e^x - 1)^2} dx$$

θ_D Debye temperature, a material's property

Nb: $T_c/\theta_D = 0.04$

Material	θ_D (K)	Material	θ_D (K)
Aluminium	385	Lead	85
Carbon (graphite)	760	Nickel	440
Copper	310	Niobium	265
Gold	180	Silver	220
Indium	105	Titanium	355
Iron	460	Quartz	255

};

Thermal Properties

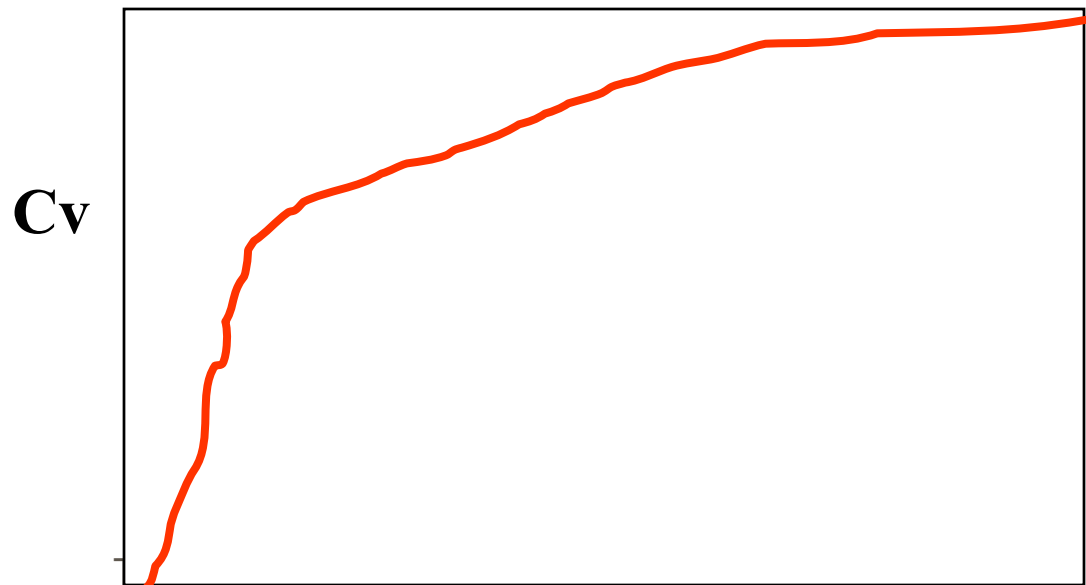
Thermal
Contraction

Energy Required to change the temperature
of 1 g substance by one degree

Specific Heat

Why do you require “Cp”?

Thermal
Conductivity



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T/ Td

Role of Specific Heat on Cool Down

To cool 1 gm mass from Room temperature to 4.2 K

$$Q = m C_p (300 - 4.2) \text{ J}, \quad C_p = f(T)$$

At low temperature C_p is less, less heat to be extracted at low Temperature

How much Cryogen (M_c) is required to cool 1 Kg mass

$$M_c \cdot L = m \cdot C_p (300 - 4.2)$$

Requirement of Cryogen To cool Down

Material	300-4.2 (L_{He})	78- 4.2 K	With cold gas (300-4.2)	300-80 (LN₂)
SS	33 litres/kg	1.44 litres/kg	0.80 litres/kg	0.53 litres/kg
Al	66	3.2	1.60	1.0

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Measuring Instruments at Low Temperature



- ⌘ **Temperature** : Platinum, Diode, Thermocouple
- ⌘ **Liquid Level** : Capacitance, Superconducting, Differential Pressure
- ⌘ **Flow rate** : Orifice meter, Turbine flow
- ⌘ **Quality** : Capacitance Type (Liquid/ gas)

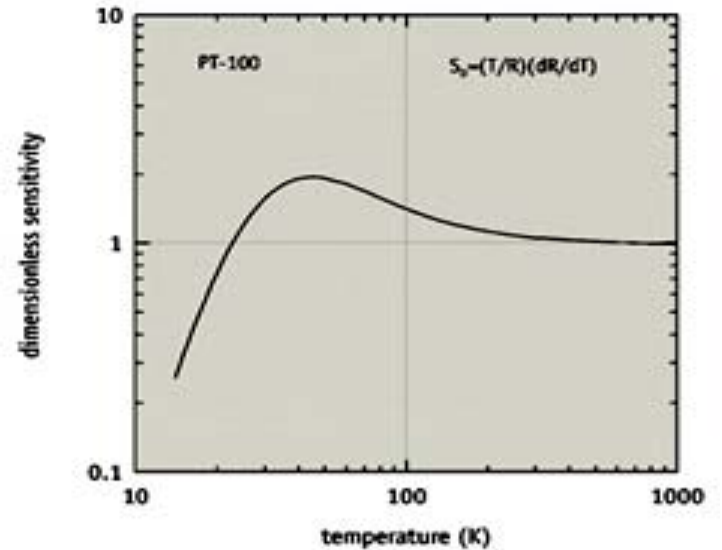
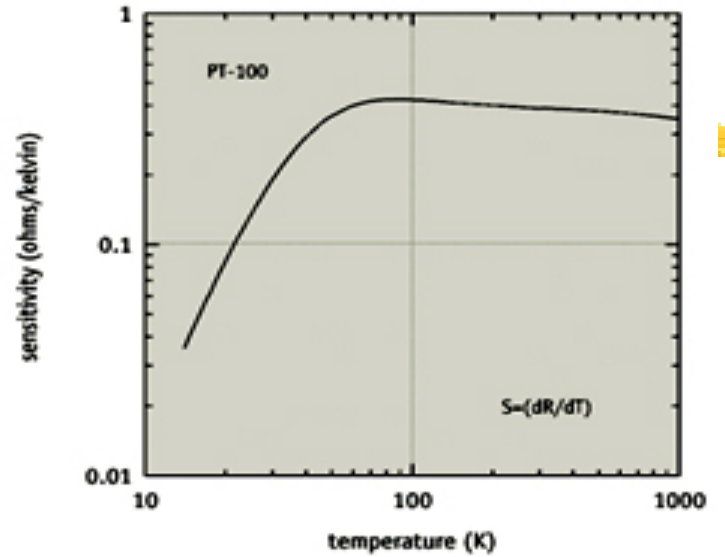
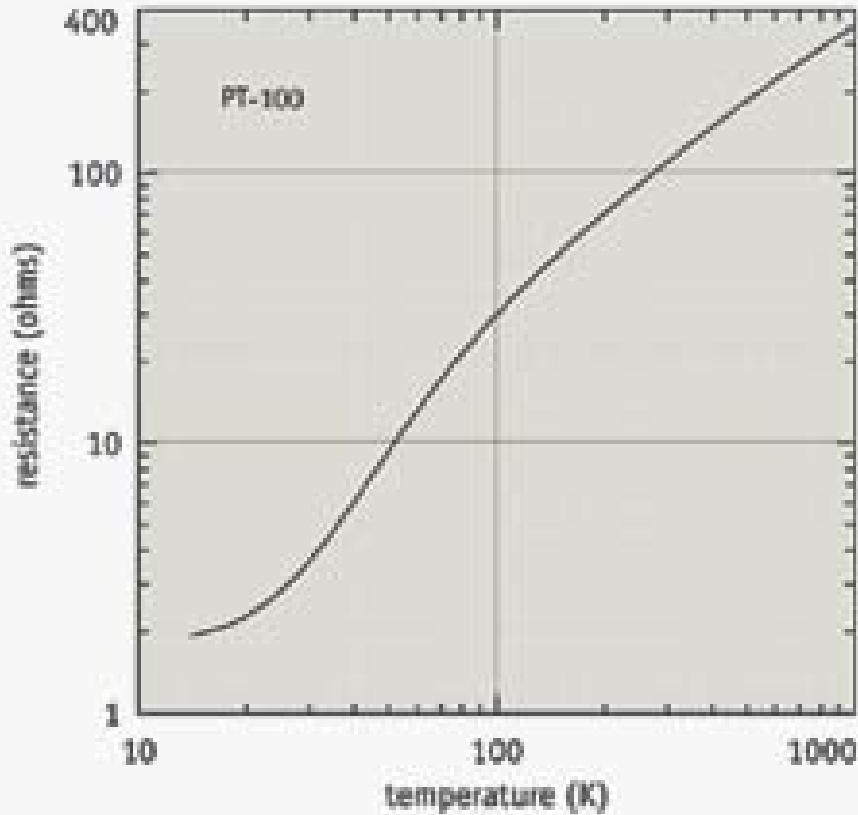
Platinum Resistance Thermometer



Platinum PT-100			
T (K)	R (Ω)	dR/dT (Ω /K)	(T/R)-(dR/dT)
20	2.2913	0.085	0.74
30	3.6596	0.191	1.60
50	9.3865	0.360	1.90
77.35	20.380	0.423	1.60
100	29.989	0.423	1.40
150	50.788	0.409	1.20
200	71.011	0.400	1.10
250	90.845	0.393	1.10
300	110.354	0.387	1.10
400	148.640	0.383	1.00
500	185.668	0.378	1.00
600	221.535	0.372	1.00
700	256.243	0.366	1.00
800	289.789	0.360	1.00

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Platinum Resistance Thermometer



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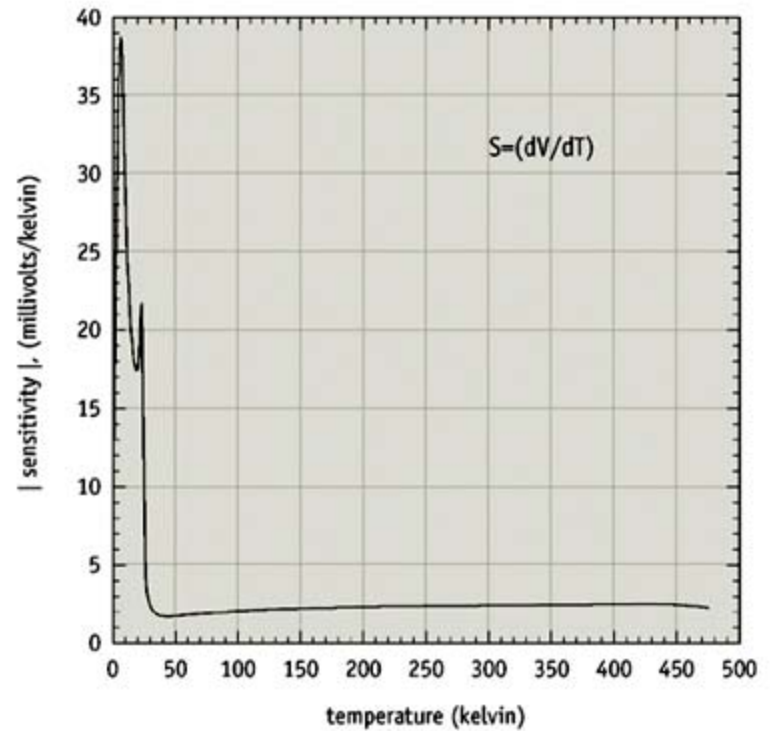
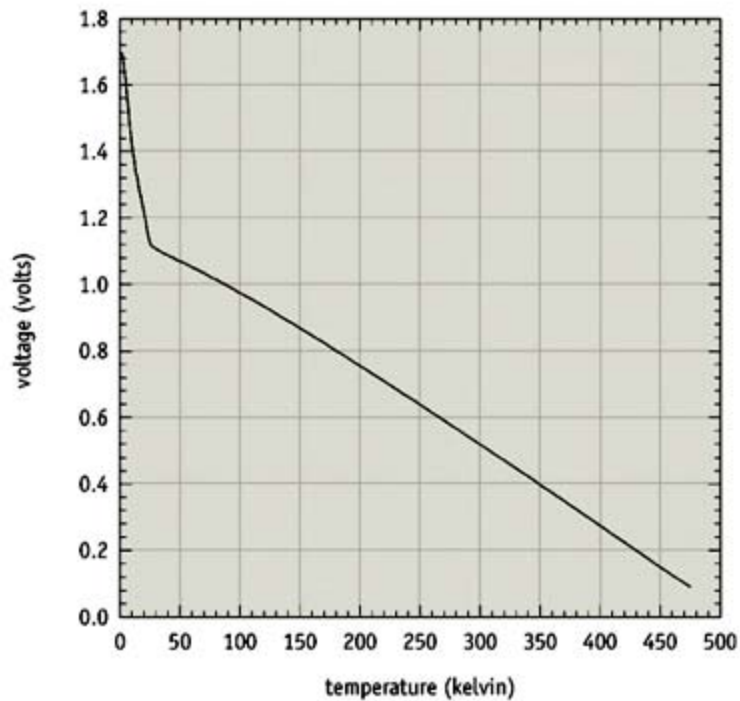
Silicone Diode Thermometer



Silicon Diode		
T (K)	V (volts)	dV/dT (mV/K)
4.2	1.6260	-33.6
10	1.4201	-28.7
20	1.2144	-17.6
30	1.1070	-2.34
50	1.0705	-1.75
77.35	1.0203	-1.92
100	0.9755	-2.04
150	0.8687	-2.19
200	0.7555	-2.31
250	0.6384	-2.37
300	0.5189	-2.4
350	0.3978	-2.44
400	0.2746	-2.49
450	0.1499	-2.46
475	0.0906	-2.22

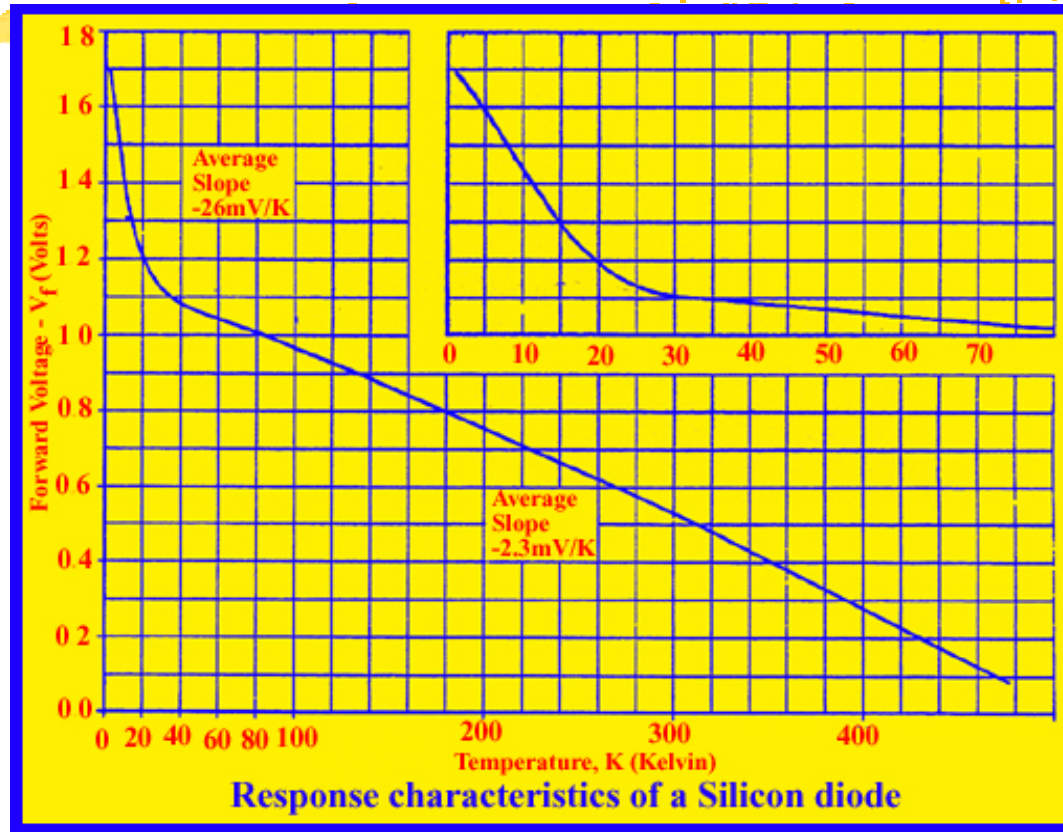
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Silicone Diode Thermometer



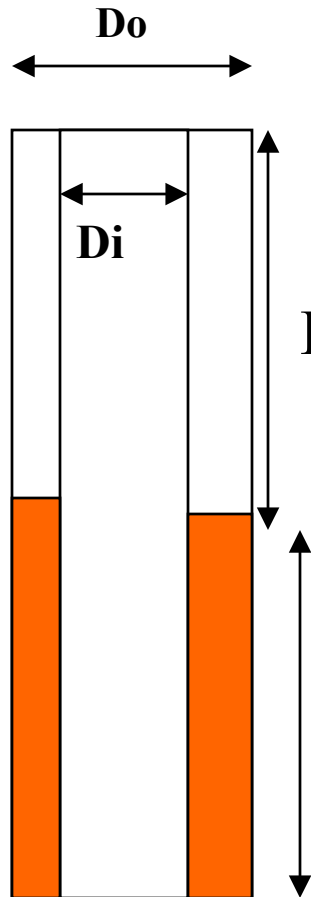
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Silicone Diode Thermometer



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LIQUID LEVEL METER



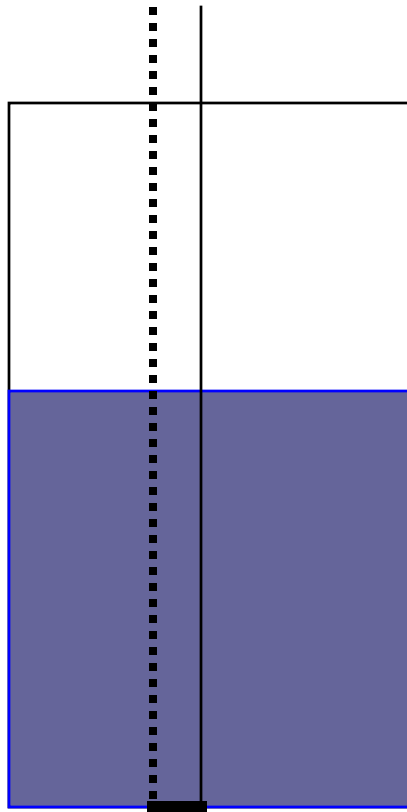
The capacitance of concentric Cylinder tube is

$$C = C_f + C_g = 2\pi (L_f \epsilon_f + L_g \epsilon_g) / \ln(D_o/D_i)$$

ϵ_f, ϵ_g : Dielectric Constant for liquid & Gas

L_f This is popular for Liquid nitrogen but not for liquid Helium

Liquid level meter by Superconducting wire



Nb- Ti Commercial wire ($T_c = 12$ K)

The length of the wire immersed in liquid helium will be superconductor. Resistance will be only for ($L - L_f$) length of wire. By measuring resistance and comparing with total resistance without liquid we will be able to calculate length of liquid helium level

HELIUM GAS STORAGE TANK AT IUAC

Storage Capacity : 2 x 40 + 1 x 60 M3

INVENTORY 2100 M3

Op. Pressure : 240 psig


Eq : 320 Cylinders

Thank You



A blue-tinted photograph of a university campus. In the background, a tall, multi-story clock tower with a square top section and arched windows stands prominently. To the right, a large, leafy tree is visible. In the foreground, there is a paved area, possibly a road or walkway, with some landscaping and a low wall. The overall scene is bright and clear.

Thank You



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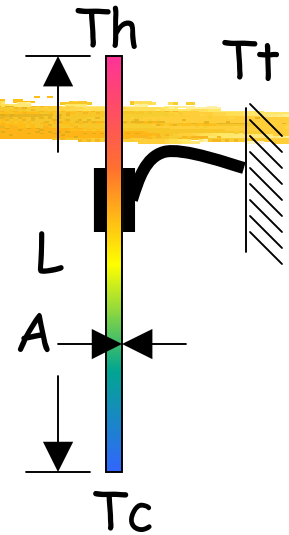
Time-independent conduction

1D, constant A

$$\dot{Q} = -k(T)A \frac{dT}{dx} \longrightarrow \dot{Q} = \frac{A}{L} \int_{T_c}^{T_h} k(T) dT$$

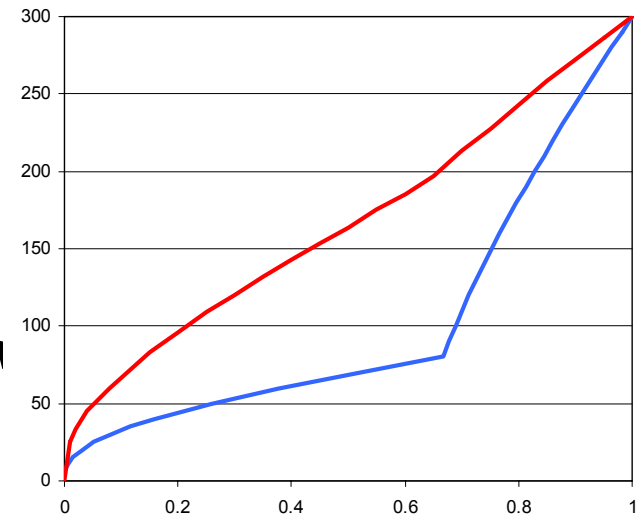
$$\int_{T_c}^{T_h} k(T) dT = \text{material's property}$$

$$G = \left(\int_{x_1}^{x_2} \frac{dx}{A(x)} \right)^{-1}$$

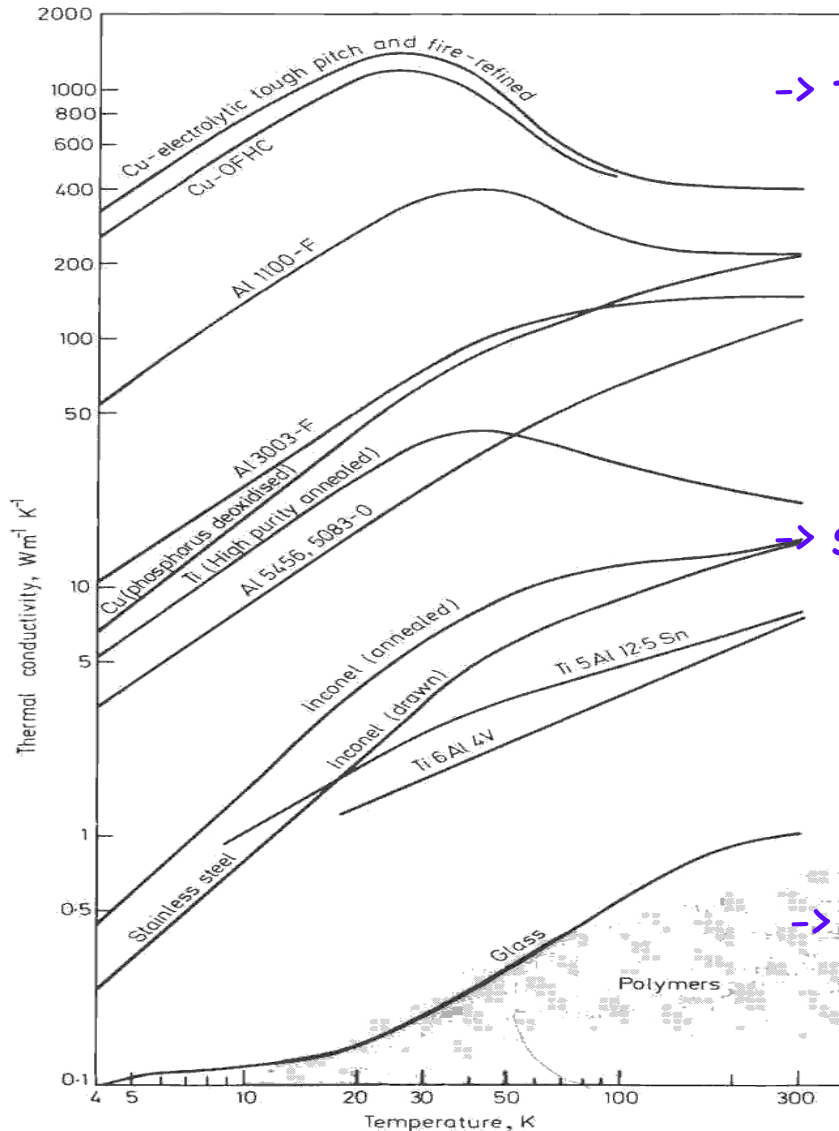


Heat flux reduction by intermediate temperature thermalization:

Temperature profile $T(x)$ of st. steel bar with thermalization 2/3 of length at 80K



Conductivity of solids



-> form for pure and alloyed metals

-> st. steel

-> increase with T

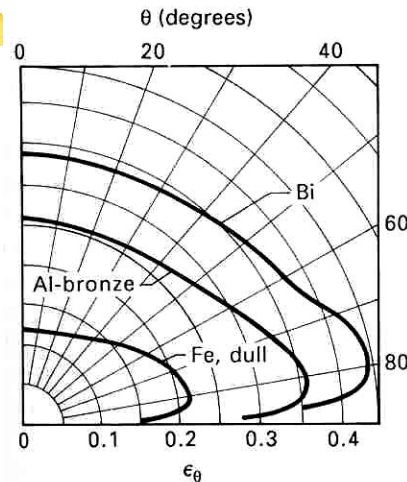
3-08 :

January 7-

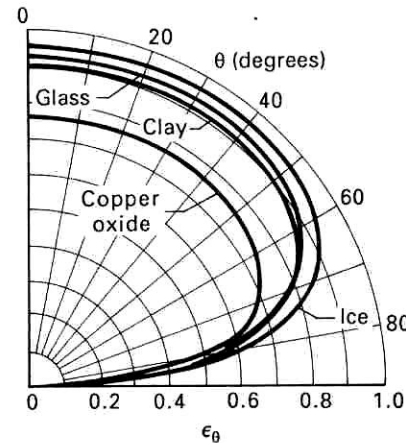
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Emissivity and materials

Real emissivities depend on direction and wavelength



(a) Metal surfaces.



(b) Electric nonconducting surfaces.

Drude law for ideal metal

$$\epsilon(\lambda, T) = 0.365 \sqrt{\frac{\rho(T)}{\lambda}}$$

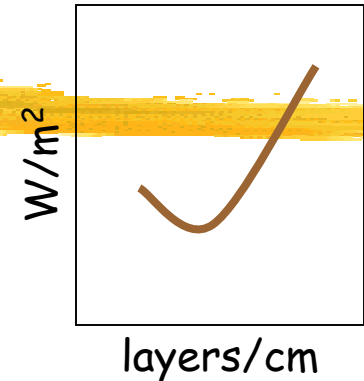
- ⌘ Polished metals: small ϵ
- ⌘ Insulators: large ϵ
- ⌘ $\epsilon = \epsilon(T)$: for real metals, $\epsilon \sim T$ at low T
- ⌘ Coatings: since ϵ related to surface, not bulk, resistance, \Rightarrow lower limit on thickness of reflectors ($\rho \approx 1$ above $\sim 40\text{nm}$)

MLI: effective conductivity

Effective conductivity $k = aT + bT^3$

Heat transfer rate $q = k/e \Delta T$, $e =$ thickness

Optimal density: $10-20 \text{ cm}^{-1}$



Low boundary temperature:

77 K \rightarrow 4K

heat transfer rate determined by aT , not by radiation

1 single aluminized foil is sufficient in high vacuum
in bad vacuum, MLI provides sufficient insulation

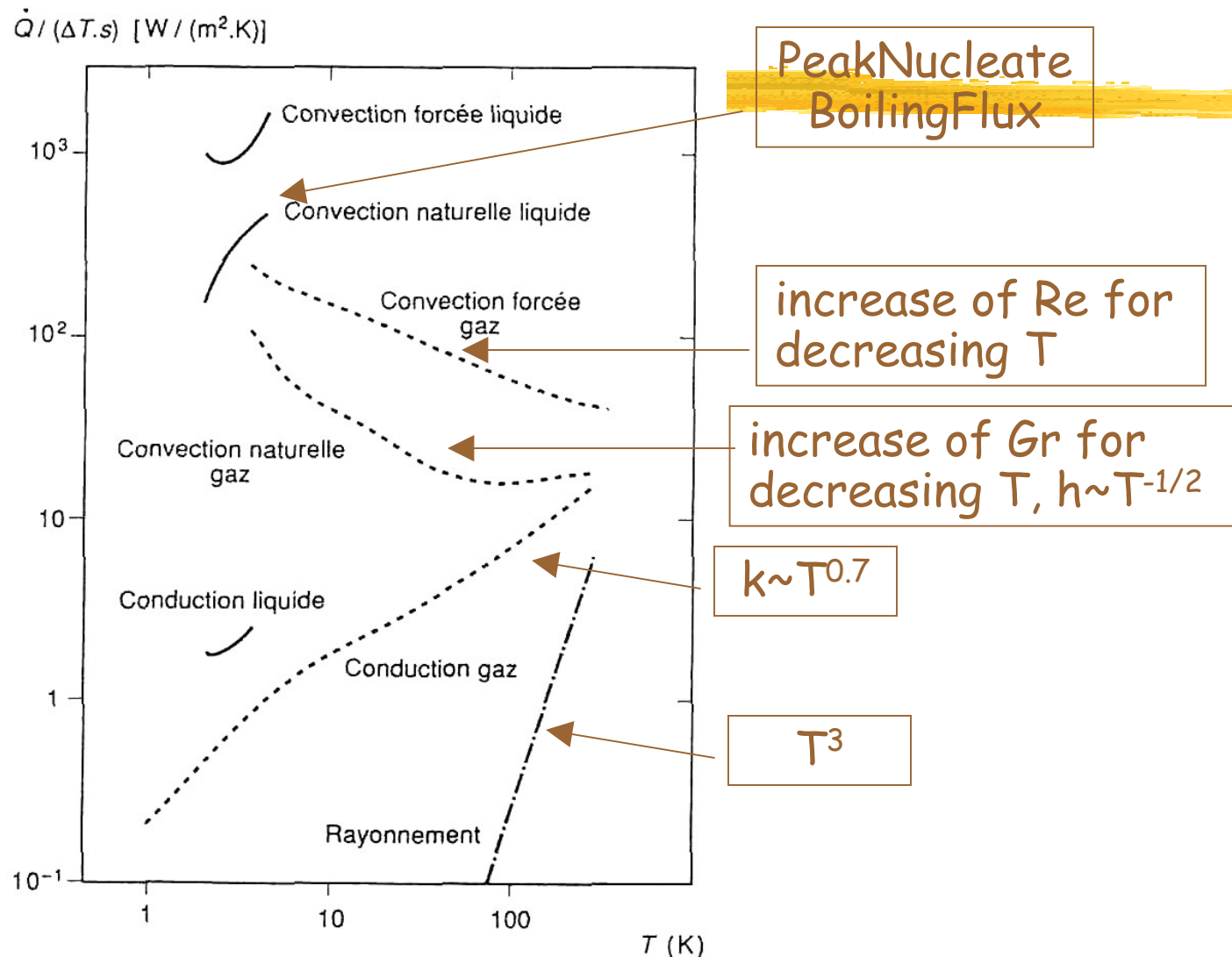
High boundary temperature:

300 K \rightarrow 77K

heat transfer rate determined by radiation
important reduction with layer's number

bad vacuum: radiation dominates anyway

Cryogenic heat transfer modes



Conductivity of solids

- ⌘ Heat carriers: phonons ($k \sim T^3$) and electrons ($k \sim T$)
- ⌘ Good electrical conductors = good thermal conductors (but not the best ones !)
- ⌘ Hinder heat transmission at low T ? **DEFECTS**
difference between pure and alloyed
effect of modification of the defect content: magnetic impurities, annealing, cold work
- ⌘ Hinder heat transmission at high T ? **Phonon-phonon**
Phonon-electron
no difference between pure and alloyed metals